

Name: _____

APPM 1350
Summer 2023

Exam 3

July 14

Instructions:

- Write your name at the top of each page.
- Show all work and simplify your answers, except where the instructions tell you to leave your answer unsimplified.
- Be sure that your work is legible and organized.
- Name any theorem that you use and explain how it is used.
- Answers with no justification will receive no points unless the problem explicitly states otherwise.
- Notes, your text and other books, calculators, cell phones, and other electronic devices are not permitted, except as needed to upload your work.
- When you have completed the exam, upload it to Gradescope. Verify that everything has been uploaded correctly and pages have been associated to the correct problem before you leave the room.
-

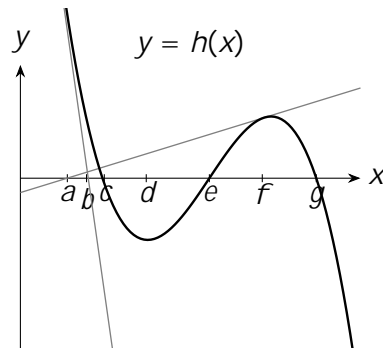
1. (28 pts) The following problems are unrelated.

(a) Find the specific form of $f(t)$ if $f^{(0)}(t) = \frac{3}{t}$, $f(1) = 6$, and $f'(1) = 3$.

(b) Given $\int_1^5 f(x) dx = 4$ and $\int_1^5 2g(x) dx = 14$, find $\int_1^5 \frac{1}{2}f(x) + 3g(x) dx$.

(c) Evaluate $\int \frac{r^3 - 2r + 1}{r^5 - 2} dr$

2. (10 pts) Suppose Newton's Method is applied to the function $h(x)$, shown below including tangent lines to the curve at certain points. Use the graph to answer the following two problems.



(a) If we chose our initial approximation x_1 to be f , what would our next approximations x_2 , and x_3 be? No justification necessary.

(b) If we chose our initial approximation x_1 to be d , would Newton's method converge, diverge, or fail? If it converges, what will it converge to? If it fails, explain why. No explanation needed if it diverges.

3. (20 pts) The following problems are unrelated.

(a) Use 4 rectangles to approximate the area under the curve for $f(x) = 1 + \cos(2x)$ on the interval $[0; \pi]$.

i. Find x and x_i , and use them to set up an expression for R_4 .

ii. Evaluate the expression found in part (i).

(b) The graph of a function g is given below on the interval $[0; 10]$. Using a Riemann sum with $n = 5$, sketch the approximating rectangles according to the right endpoints. DO NOT evaluate the sum.

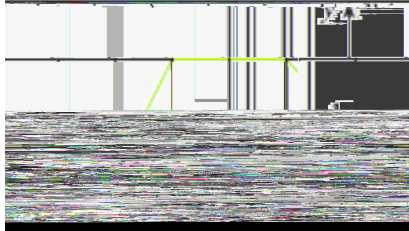


4. (18 pts) Evaluate each of the following definite integrals.

(a) $\int_{-2}^2 \frac{\cos(1-x)}{x^2} dx$

(b) $\int_{-2}^2 x^4 \tan \frac{x}{1+x^2} + \int_0^1 \frac{p(x)}{4-x^2} dx$ (Hint: Do not attempt to find any antiderivatives.)

5. (24 pts) Consider the continuous function $p(t)$ defined on $[0; 6]$, shown below, for the following questions.



(a) Find the average value of p on the interval $[2; 6]$

(b) Let $q(x) = x^2 + \int_0^{x^2} p(t) dt$ where p is still given by the graph above.

i. Find $q(2)$.

ii. Find $q'(2)$.

THIS IS THE END OF THE EXAM